

## Communications to the Editor

### On Binding Forces between Aromatic Ring and Quaternary Ammonium Compound

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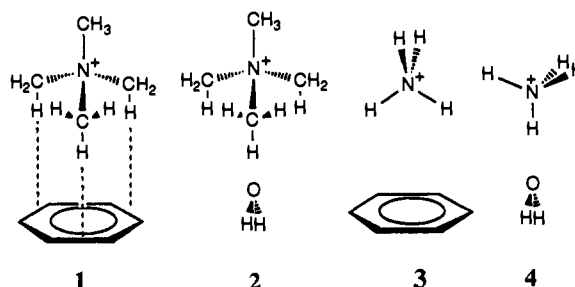
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Recently, the cation- $\pi$  interaction has received considerable attention as a new type of binding force that is important in biological systems. Several propositions have been formulated on the basis of experimental findings and theoretical calculations on the nature of the force at the molecular level.<sup>1-3</sup> Of these, the proposition of Dougherty et al.<sup>2</sup> is of particular interest. According to them the cation- $\pi$  interaction is responsible for not only the ion selectivity of potassium channel but also the binding of acetylcholine (ACh) to its deactivating enzyme, acetylcholinesterase (AChE). This enzyme has long been served as a target molecule in designing potential therapeutic agents of various ailments such as myasthenia gravis, glaucoma, and possibly Alzheimer's disease.<sup>4</sup> Until recently, it was generally believed that at the active site of AChE there is present an anionic subsite consisting of carboxylate groups, which accommodates the charged quaternary moiety of the neurotransmitter.<sup>4c</sup> But, recent X-ray structure analysis of AChE revealed that at the active site there are 14 aromatic amino acid residues but no more than one acidic group which is slightly far from the charged moiety in a protonated form or with a counterion nearby.<sup>3</sup>

In an effort to shed light on the character of the binding forces of ACh to AChE as well as to better understand the nature of

the cation- $\pi$  interaction, we carried out extensive *ab initio* calculations for the complexes of tetramethylammonium cation ( $\text{Me}_4\text{N}^+$ ) with benzene (**1**) and with water (**2**), and the complexes of ammonium cation ( $\text{H}_4\text{N}^+$ ) with benzene (**3**) and with water (**4**). The calculations involve the Hartree-Fock (HF) and Møller-Plesset second-order perturbation (MP2) treatments with 6-311+G\*\* basis sets at optimized geometries using Gaussian 92,<sup>5</sup> and the results are summarized in Table 1.



It is seen that the MP2-predicted enthalpy and free energy changes ( $\Delta H_r$ ,  $\Delta G_r$ ) for the complex formations agree reasonably well with the experimental data.<sup>6</sup> In the case of **2** the charge-dipole interaction ( $\Delta E_{+, \mu} = -9.8$  kcal/mol) constitutes a major binding force. In the case of **1** not only the charge-quadrupole ( $\Delta E_{+, Q} = -7.7$  kcal/mol) and charge-polarizability ( $\Delta E_{+, \alpha} = -3.2$  kcal/mol) interactions but also the electron correlation effect ( $\Delta E_{\text{cor}} = -8.4 \pm 1.5$  kcal/mol) is important. From the comparison of the HF and MP2 results, we find that the electron correlation effect enhances the interaction energies of  $\Delta E_{+, Q}$  and  $\Delta E_{+, \alpha}$  by 1.5 and 1.1 kcal/mol, respectively. The sum of the electrostatic interaction energy ( $\Delta E_{\text{es}}$ ) and  $\Delta E_{\text{cor}}$  is much larger in magnitude than the binding energy ( $\Delta E^{\text{N}}$ ). A major portion of this energy difference ( $\sim 7.6$  kcal/mol) is likely to be due to the exchange repulsion (see footnote *f* of Table I).

The large difference between the HF and MP2 results, large  $\Delta E_{\text{cor}}$ , arises mostly because a small fraction of the LUMO electron clouds is taken into account in the MP2 results, but not in the HF results. In the  $\pi$ -LUMOs of **1** the  $\pi$  orbital lobes are much highly prolate from benzene to  $\text{Me}_4\text{N}^+$  compared with those in the HOMO (Figure 1).<sup>7</sup> The repulsive interaction between the delocalized  $\pi$  electron clouds over the benzene ring and the electron clouds of  $\text{Me}_4\text{N}^+$  tends to be mitigated through a transfer of the  $\pi$  electrons in the benzene ring to the  $\sigma_{\text{C-H}}^*$  orbitals in  $\text{Me}_4\text{N}^+$ , (i.e.,  $\pi$ - $\sigma^*$  through-space interaction, which is a very novel type of interaction). Namely, a portion of the  $\pi$ -LUMO electron clouds surrounds the partially positively charged H atoms in  $\text{Me}_4\text{N}^+$ , so that  $\Delta E_{\text{cor}}$  contributes significantly in the binding of  $\text{Me}_4\text{N}^+$  to benzene.

On the other hand, in the case of **2** the hydrogen atoms in  $\text{Me}_4\text{N}^+$  approach to the electron-donating lone pair electrons localized around the oxygen nucleus of  $\text{H}_2\text{O}$ , which results in a  $\sigma$  electron transfer. Owing to the lack of  $\pi$ -electrons in **2** and **4**, their  $\Delta E_{\text{cor}}$  are small ( $-2.9 \pm 0.9$  kcal/mol and  $-2.6 \pm 1.0$  kcal/mol, respectively). In comparison,  $\Delta E_{\text{cor}}$  for **3** ( $-6.2 \pm 1.1$  kcal/mol) is large but smaller (by  $\sim 2.2$  kcal/mol) in magnitude than that for **1**, because the  $\pi$  and  $\sigma_{\text{C-H}}^*$  orbitals in **1** are lined up to

(5) Frisch et al. *Gaussian 92*; Gaussian, Inc.: Pittsburgh, 1992.

(6) Meot-Ner (Mautner), M.; Deakyne, C. A. *J. Am. Chem. Soc.* **1985**, *107*, 469-474.

(7) The first LUMO is a  $\sigma$  orbital and the second LUMOs are degenerate  $\pi$  orbitals. Since the enhancement of charge-polarizability interaction by electron correlation arises mainly from an easy transfer of the delocalized  $\pi$  electrons from the HOMOs to LUMOs, one of the degenerate  $\pi$ -LUMOs is shown.

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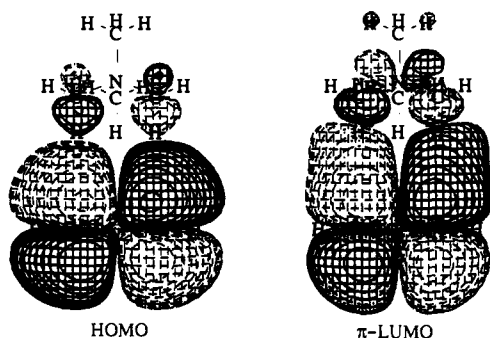
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Table 1. Complexation Energies of 1–4<sup>a</sup>

	1	2	3	4
$\Delta E_{\text{e}}^{\text{N}}$	-11.72	-11.52	-18.97	-21.70
$\Delta E_{\text{e}}^{\text{B}}$	-8.67	-9.72	-16.88	-19.76
$\Delta E_{\text{e}}$	-10.20 ± 1.53	-10.62 ± 0.90	-17.93 ± 1.05	-20.73 ± 0.97
$\Delta E_0$	-9.66 ± 1.53	-8.98 ± 0.90	-16.99 ± 1.05	-18.93 ± 0.97
$\Delta H_{\text{T}}$	-9.49 ± 1.53	-8.95 ± 0.90	-16.75 ± 1.05	-18.85 ± 0.97
$\Delta H_{\text{T}}^{\text{exp } b}$	-9.4 ± 1.	-9.0 ± 1.	-19.3 ± 1. <sup>c</sup>	
$\Delta G_{\text{T}}^d$	-4.08 ± 1.53	-3.61 ± 0.90	-12.79 ± 1.05	-13.87 ± 0.97
$\Delta G_{\text{T}}^{\text{exp } b}$	-3.5	(-2.6 ± 1.6)	(-12.4 ± 1.6) <sup>c</sup>	
$d_{\text{N-R}}^e$	4.217	3.936	2.915	2.993
$\Delta E_{+\mu}$	0.00	-9.78	0.00	-16.91
$\Delta E_{+Q}$	-7.71	-0.37	(-23.35)	-0.85
$\Delta E_{+\alpha}$	-3.23	-0.53	(-6.88)	-1.58
$\Delta E_{\alpha\mu}$	0.00	-0.25	0.00	-0.20
$\Delta E_{\text{es}}$	-10.94	-10.93	(-30.23)	-19.54
$\Delta E_{\text{cor}}^f$	-4.71 ± 1.53	-1.55 ± 0.90	-3.64 ± 1.05	-1.49 ± 0.97
$\Delta E_{\text{cor}}$	-8.40 ± 1.53	-2.89 ± 0.90	-6.19 ± 1.05	-2.56 ± 0.97

<sup>a</sup> All energies are given in kcal/mol.  $\Delta E_{\text{e}}^{\text{N}}$  and  $\Delta E_{\text{e}}^{\text{B}}$  denote the binding energies without and with basis set superposition error (BSSE) correction, respectively. Although the latter energy is generally accepted to be more reliable, there is a trend that the latter is still underestimated, while the former is overestimated.<sup>8</sup> Thus, the median value plus/minus a half value of the BSSE,  $\Delta E_{\text{e}}$ , was chosen to represent both  $\Delta E_{\text{e}}^{\text{B}}$  and  $\Delta E_{\text{e}}^{\text{N}}$  as the upper and lower bounds, respectively. All other thermodynamic quantities were represented in the same way:  $\Delta E_0$  is the zero point energy, while  $\Delta H_{\text{T}}$  and  $\Delta G_{\text{T}}$  are the enthalpy and Gibbs free energy at 1 atm and 298 K, respectively. All geometries were optimized with MP2/6-311+G\*\* calculations. To obtain thermal energies, the MP2/6-31G\* vibrational frequencies were used for all the complexes except for 1 for which the MP2/6-31G frequencies were used due to the calculational limitation. Each contribution term for the electrostatic interactions between  $\text{Me}_4\text{N}^+/\text{H}_4\text{N}^+$  and  $\text{C}_6\text{H}_6/\text{H}_2\text{O}$  is denoted by  $\Delta E_{+\mu}$ ,  $\Delta E_{+Q}$ , and  $\Delta E_{+\alpha}$  in which the first subscript denotes the + charge in  $\text{Me}_4\text{N}^+/\text{H}_4\text{N}^+$ , while the second subscript denotes the dipole, quadrupole, and polarizability in  $\text{C}_6\text{H}_6/\text{H}_2\text{O}$ , respectively.  $\Delta E_{\alpha\mu}$  is the interaction energy between the polarizability of  $\text{Me}_4\text{N}^+/\text{H}_4\text{N}^+$  and the dipole of  $\text{C}_6\text{H}_6/\text{H}_2\text{O}$ . Since the electrostatic interactions due to high multipole moments and hyperpolarizabilities are either zero or negligible, the total electrostatic interaction energy ( $\Delta E_{\text{es}}$ ) is approximately the sum of  $\Delta E_{+\mu}$ ,  $\Delta E_{+Q}$ ,  $\Delta E_{+\alpha}$ , and  $\Delta E_{\alpha\mu}$ , unless there is not much molecular orbital interaction in complexation. (But, for a complex like 3 in which the two inner molecules are separated only by a short distance with high redistribution of electrons, the multipole expansion may not be a useful representation; thus, the corresponding values are given in parentheses. <sup>b</sup> Experimental values from ref 6.  $\Delta G_{\text{T}}^{\text{exp}}$ 's in parentheses were estimated from the experimental enthalpy and estimated entropy with the errors of 1 kcal/mol and 2 cal/mol/K, respectively. <sup>c</sup> From Figure 1 in ref 6, one can note that the slope of the van't Hoff plots was to be drawn somewhat steep near room temperature region, indicating that the value of -19.3 is likely to be reduced down to -17. <sup>d</sup>  $\Delta G_{\text{T}}$ 's are not reliable enough due to a few low frequency modes. The lowest frequency mode of 1/3 was treated as internal free rotation by  $\text{C}_6\text{H}_6$  and  $\text{Me}_4\text{N}^+/\text{H}_4\text{N}^+$  at room temperature. <sup>e</sup>  $d_{\text{N-R}}$  is the distance (Å) between N and the centroid of benzene-quadrupole/water-dipole. <sup>f</sup> The electron correlation energies are defined as follows.  $\Delta E_{\text{cor}}^f/\Delta E_{\text{cor}}$  is the value of  $E_{\text{c}}(\text{MP2})$  at the MP2 optimized geometry subtracted by  $E_{\text{c}}(\text{HF})$  at the HF/MP2 optimized geometry. Since the benzene complexes have high repulsive energies between the benzene  $\pi$ -electrons and the countermolecule electrons, the complex structure at the MP2 optimized geometry is located at highly repulsive hard wall potential region at the level of the HF theory. This results in a large electron correlation energy difference between  $\Delta E_{\text{cor}}^f$  and  $\Delta E_{\text{cor}}$ . Since the MP2 structure should be considered much more realistic, only  $\Delta E_{\text{cor}}$  is discussed in the text.

Figure 1.  $\pi$ -LUMO and HOMO of the complex of  $\text{Me}_4\text{N}^+$  with benzene.

give the maximum overlap, while the  $\pi$  and  $\sigma_{\text{N-H}}^*$  orbitals in 3 are tilted. Further, the portion of  $\Delta E_{\text{cor}}$  in the binding is much smaller in 3 than 1. Apparently, since the positive charge enhances polarizability and charge transfer in the  $\pi$ -LUMO,  $\Delta E_{\text{cor}}$  becomes much larger in magnitude than the ordinary dispersion energy between neutral molecules.

In conclusion, the results of our *ab initio* calculations confirm that the important binding forces in the complexing of  $\text{Me}_4\text{N}^+$  with benzene arises from the charge-quadrupole and charge-polarizability interactions in agreement with the proposition of Dougherty and Stauffer.<sup>2a</sup> What is even a more important finding

for the binding is that  $\Delta E_{\text{cor}}$  is as important as the charge-quadrupole interaction and plays a key role in the binding so that  $\text{Me}_4\text{N}^+$  binds benzene slightly more strongly than water. This is important, considering the fact that  $\text{H}_4\text{N}^+$  binds water more strongly than benzene. Apparently, a tetramethyl quaternary ammonium ion is an exceptional cation that forms a complex efficaciously with aromatic rings, and now we may understand why nature has chosen a cation such as ACh for interaction with aromatic rings in AChE. Finally, the present study may provide a theoretical background for designing of efficient aromatic host-charged guest supramolecules.<sup>9</sup>

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